

Nonlinear Energy Harvesting

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Noise in Physical Systems

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Noise energy harvesting

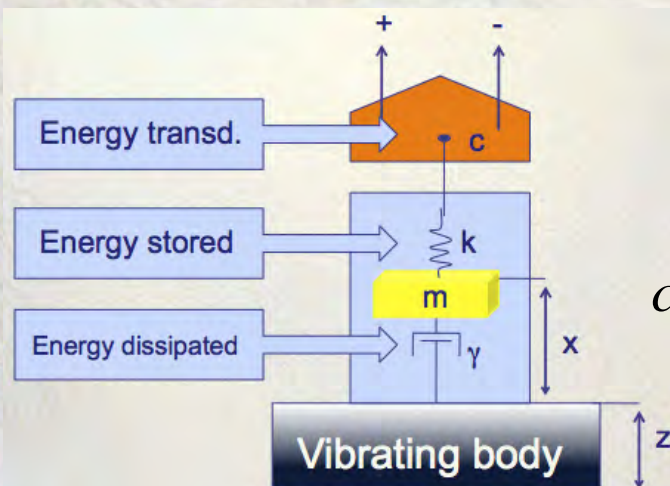
Dynamical model for a vibrational energy harvester

$$m\ddot{x} = -\frac{dU(x)}{dx} - \gamma\dot{x} - c(x,V) + \xi_z$$

$$\dot{V} = F(\dot{x}, V)$$

Details depend on the physics...

Equations that link the vibration-induced displacement with the Voltage



$U(x)$ Represents the Energy stored

$\gamma\dot{x}$ Accounts for the Energy dissipated

$c(x,V)$ Accounts for the Energy transduced

ξ_z Accounts for the input Energy

Noise energy harvesting

Transduction mechanisms

1

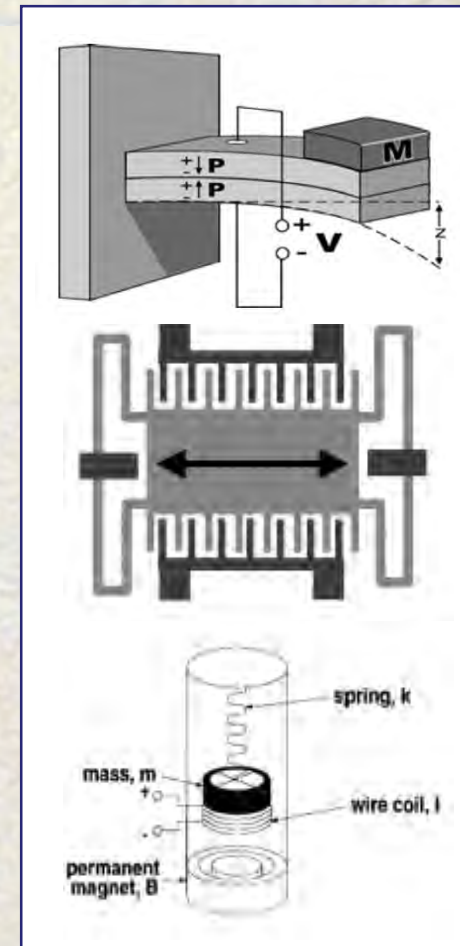
Piezoelectric: dynamical strain is converted into voltage difference.

2

Capacitive: geometrical variations induce voltage difference

3

Inductive: dynamical oscillations of magnets induce electric current in coils



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Transduction mechanisms

1

Piezoelectric: dynamical strain is converted into voltage difference.

$$m\ddot{x} = -\frac{dU(x)}{dx} - \gamma\dot{x} - K_V V + \xi_z$$

$$\dot{V} = K_c \dot{x} - \frac{1}{\tau_p} V$$

The Physics of piezo materials

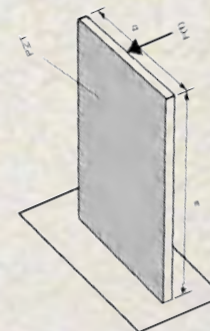
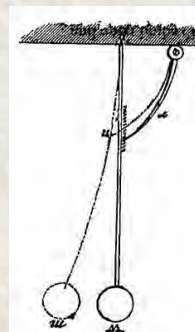
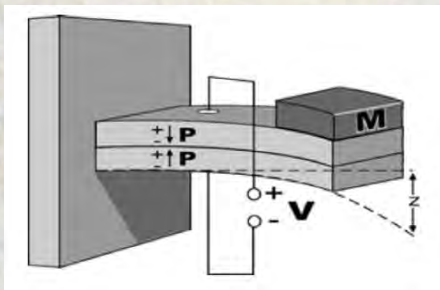
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Linear systems

When $U(x) = \frac{1}{2}kx^2$ it is called a linear system

Linear systems have some interesting features... (and people like them most)

- 1) There exist a simple math theory to solve the eq.s
- 2) They have a resonant behaviour (resonance freq.)
- 3) They can be “easily” realized with catilevers and pendula



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Linear systems

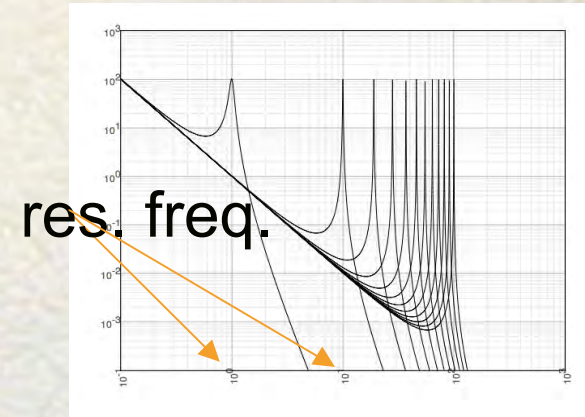
For a linear system the transfer function presents one or more peaks corresponding to the resonance frequencies and **thus it is efficient mainly when the incoming energy is abundant in that regions...**

This is a serious limitation when you want to build a small energy harvesting system...

Why ?!!

For two main reasons...

- The frequency spectrum of available vibrations instead of being sharply peaked at some frequency is usually very broad.
- The frequency spectrum of available vibrations is particularly rich in energy in the low frequency part... and it is very difficult, if not impossible, to build small low-frequency resonant systems...



Noise energy harvesting

Wish list for the perfect vibration harvester

- 1) Capable of harvesting energy on a broad-band
- 2) No need for frequency tuning
- 3) Capable of harvesting energy at low frequency



- 1) Non-resonant system
- 2) "Transfer function" with wide frequency resp.
- 3) Low frequency operated

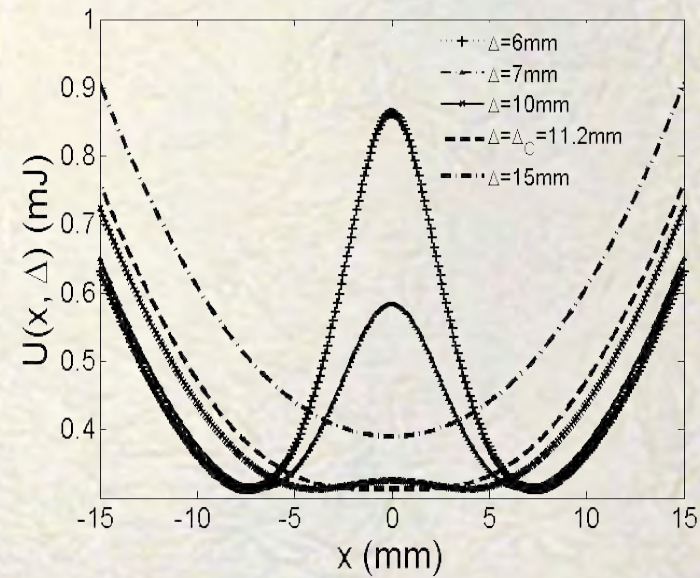
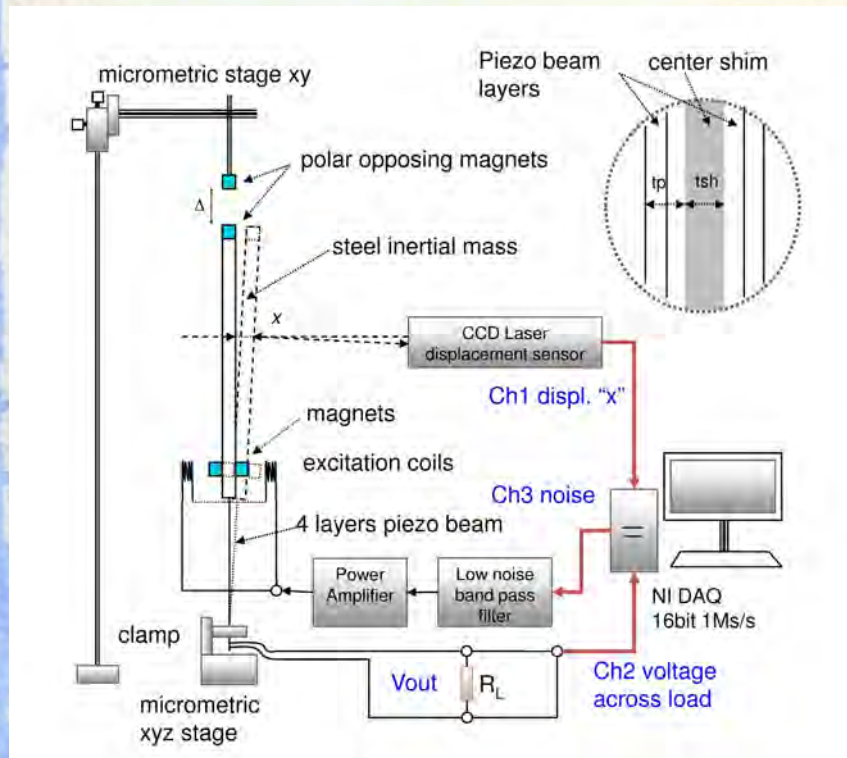


NON-Linear mechanical oscillators

- 1) Non-resonant system
- 2) "Transfer function" with wide frequency resp.
- 3) Low frequency operated

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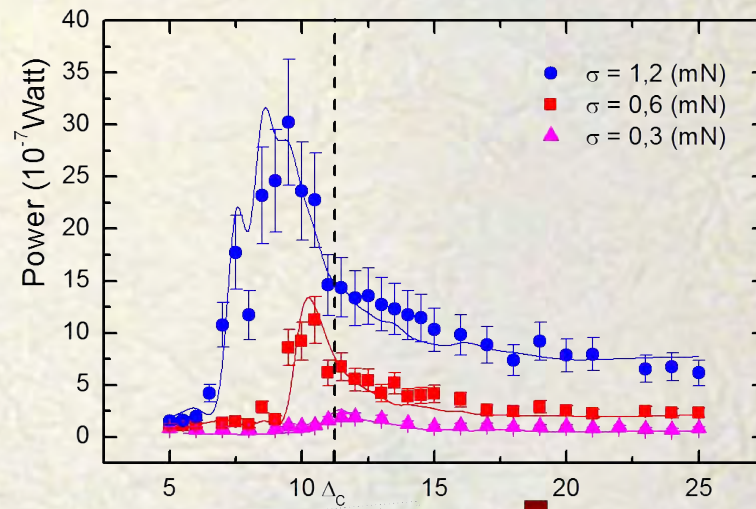
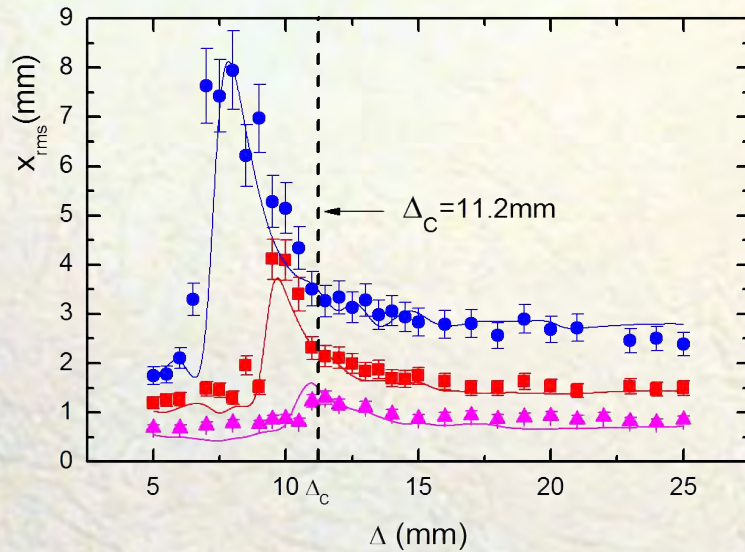
NON-Linear mechanical oscillators



Nonlinear Energy Harvesting, F. Cottone; H. Vocca; L. Gammaitoni
Physical Review Letters, 102, 080601 (2009)

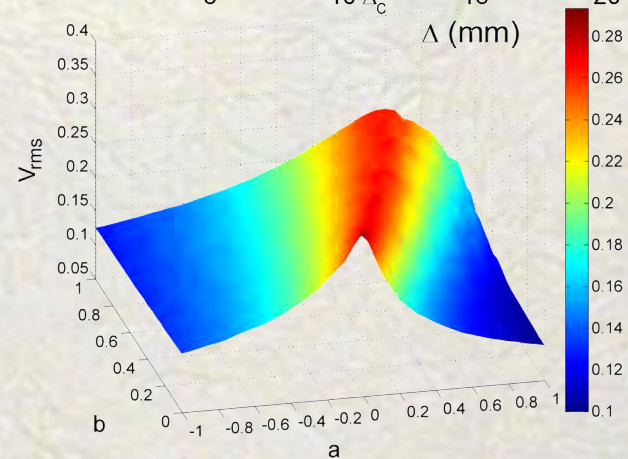
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NON-Linear mechanical oscillators



Duffing potential

$$U(x) = -\frac{1}{2}ax^2 + \frac{1}{4}bx^4$$



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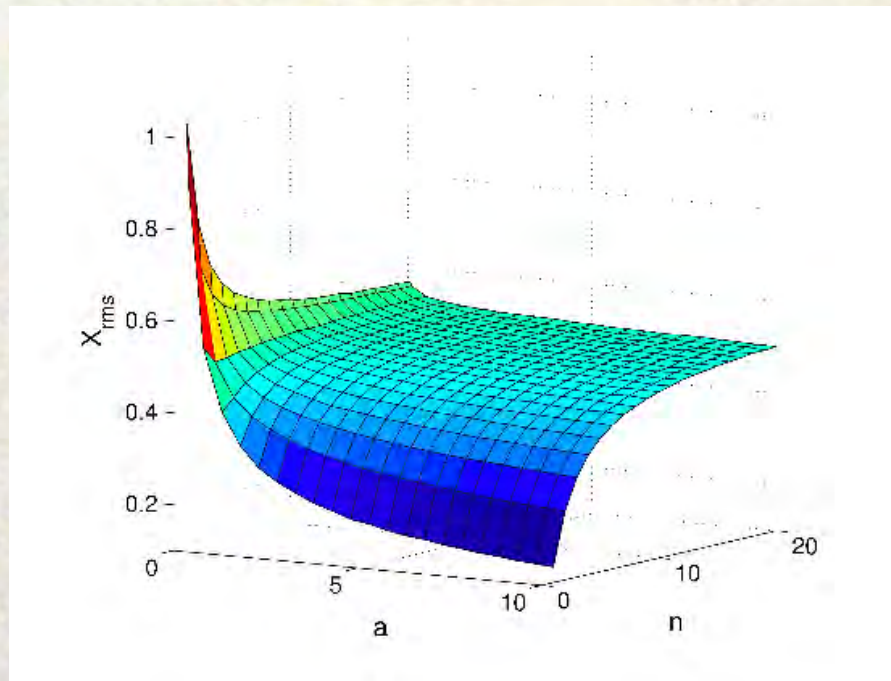
Only bistability???

A more general monostable potential...

$$U(x) = ax^{2n}$$

with : $a > 0$

$n = 1, 2, \dots$



$$a_{th} \approx \frac{D}{4} = \sigma^2 \tau$$

To think about...

- 1) Non resonant (i.e. non-linear) mechanical oscillators can outperform resonant (i.e. linear) ones*
- 2) Non-linear systems are more difficult to treat
- 3) Bistability is not the only nonlinearity available...

and

An Iphone application is pending...

* **wisepower technology** patent. For more info see: www.nipslab.org, www.wisepower.it